A High-Power Automatic Network Analyzer for Measuring the RF Power Absorbed by Biological Samples in a TEM Cell

JOHN R. JUROSHEK AND CLETUS A. HOER

Abstract — A device for measuring the radiofrequency (RF) power absorbed by biological samples while they are being irradiated in a transverse electromagnetic (TEM) cell is described. The report discusses the design, calibration, and performance of this automated measurement system. The power absorption analyzer is based on a six-port type of automatic network analyzer, and operates at an incident power to the TEM cell of 1 to 1000 W, over a frequency range of 100 to 1000 MHz. Experiments show that an absorbed power of 0.02 to 0.05 percent of the incident power can be measured. Measurements of the power absorbed by a 1-percent saline solution were made using the power absorption analyzer and by an independent calorimetric measurement. The two measurement techniques show excellent agreement.

Key Words — Automatic network analyzer, biological effects, impedance measurements, power absorption analyzer, power measurements, six-port network analyzer, and TEM cell.

I. INTRODUCTION

This report describes an RF power-absorption analyzer developed by the National Bureau of Standards for the National Institute for Occupational Safety and Health. The analyzer is designed specifically to measure the power absorbed by biological samples while they are being irradiated with continuous-wave RF energy in a transverse electromagnetic (TEM) cell. The analyzer is based on a six-port automatic network analyzer which makes it possible to detect very small amounts of absorbed power [1]–[3]. Typically, the incident power to the TEM cell is of the order of 1 to 1000 W over a frequency range of 100 to 1000 MHz. The goal of the power absorption analyzer is to be able to detect absorbed power levels of the order of 0.05 percent of the incident power (0.002 dB in insertion loss). Some of the problems typically encountered in making these measurements are discussed in a publication by Hill [4].

II. THEORY

A simple expression for the RF power absorbed by any biological sample irradiated in a TEM cell is derived as follows. Referring to Fig. 1 for a definition of terms, the RF power absorbed by the empty cell can be written

$$P_{cell} = P_1 - P_L = P_1(1 - \eta)$$

(1)

where

$$P_1 = \text{net power into the empty TEM cell measured at the input to the TEM cell},$$

$$P_L = \text{net power into the load measured at the output of the TEM cell},$$

$$\eta = P_L/P_1 = \text{efficiency of the empty TEM cell}.$$
When the sample is placed in the cell, the power absorbed by the sample and the cell is given by

\[ P_{\text{cell}} + P_{\text{sample}} = P_1' - P_L = P_1'(1 - \eta') \]  

(2)

where the prime indicates measurements with the sample inserted. Equation (1) shows that the power absorbed by the cell is proportional to \( P_1 \). When \( P_1 \) changes to \( P_1' \), \( P_L \) changes

\[ P_{\text{cell}}' = P_1'(1 - \eta'). \]  

(3)

Solving (2) and (3) for the power absorbed by the sample yields

\[ P_{\text{sample}} = P_1' \eta - \frac{\eta'}{b_2/a_1}. \]  

(4)

A general equation for the efficiency of any 2-port is given by Kerns and Beatty [5] as

\[ \eta = \frac{P_L}{P_1'} = \frac{b_2^2}{a_1^2} \frac{1 - |\Gamma_L|^2}{1 - |\Gamma_1|^2}. \]  

(5)

\( \Gamma_L \) = reflection coefficient of the load as seen from the output port,
\( \Gamma_1 \) = reflection coefficient looking into the empty TEM cell,
\( b_2/a_1 \) = ratio of the voltage wave emerging from the cell to the voltage wave incident on the cell.

A similar expression with primes gives \( \eta' \). The power absorption analyzer measures \( P_1' \) and all of the quantities in (5) to determine \( \eta \) and \( \eta' \). The power absorbed by the sample is then calculated from (4). These equations assume that the power absorbed by the empty cell does not change when the sample is inserted.

**III. SYSTEM DESCRIPTION**

There are undoubtedly many methods for making the measurements described in (4) and (5). The choice of a six-port network analyzer was based on a number of considerations. One reason was the data supporting its ability to make accurate, repeatable measurements [6]. Another consideration was the requirement to accurately calibrate the system from existing standards as will be discussed later. Simplicity of design, cost, and availability of hardware were also factors. Perhaps a slightly more obscure reason in favor of the six-port analyzer was the available redundancy that makes it easier to detect some types of malfunctions and to determine when the system is out of calibration.

A block diagram of the power absorption analyzer is shown in Fig. 2. Basically, the high-power RF signal is coupled to transfer switch T1, which directs the signal to either measurement port 1 or port 2. High-power, 30-dB couplers C1, C2, C3, and C4 divert part of the signal to transfer switches T2, T3, and the vector voltmeter portion of the system. Attenuators A1 and A2 are 10-dB step attenuators used for the low (below 20 W), medium (20 to 200 W), and high (200 to 1000 W) power ranges. Couplers C5 and C6 are 10-dB couplers which, along with the diode detectors and meters, provide a visual indication of the RF power. Loads Z1, Z2, Z3, and Z4 are used in the calibration process and will be described in more detail later in the report.

Loads Z5 and Z6 are 50-Ω terminations. Fig. 3 summarizes the different system configurations possible during normal operation. In Fig. 3, \( a_1 \), \( b_1 \), \( a_2 \), and \( b_2 \) are the waves at measurement ports 1 and 2.

Referring to Fig. 2, the vector voltmeter portion of the system is comprised of two power dividers (D), three 180° hybrids (H), and one 90° hybrid (Q). These hybrids and power dividers provide six signals, \( P_1 \) through \( P_6 \), that are different combinations of the waves into the vector voltmeter. The signal at \( P_1 \) is primarily a function of the signal through C6, while \( P_6 \) is primarily coupled to the signals through C5. Detectors \( P_1' \), \( P_2' \), \( P_3' \), \( P_4' \), and \( P_5' \) are equally coupled to both signals into the vector voltmeter.

The magnitude of the six signals \( P_1 \) through \( P_6 \) is measured with thermistor power detectors. Accurate power measurements are made using power meters of the NBS, type IV design [7]. For the measurements shown in Fig. 3, only power detectors \( P_1' \), \( P_2' \), \( P_3' \), and \( P_4' \) are used. These detectors provide sufficient information, according to six-port theory, to calculate the complex ratios \( a_1/b_1 \), \( a_2/b_1 \), \( a_2/b_2 \), and \( a_1/b_2 \), as shown in Fig. 3. Power detectors \( P_5' \) and \( P_6' \) are used primarily as monitoring and debugging aids.

The analyzer is entirely automated and controlled by a desktop computer. The dc voltages from the type IV power meters are read into the computer using two commercial 6-1/2-digit voltmeters. Two voltmeters are used here to reduce the effects of source-power fluctuations. Another major portion of the system is an automated commercial scanner used to switch the various components of the system.

The vector voltmeter portion of the analyzer, along with the thermistors, is packaged in a double-insulated, thermally controlled box. The inner portion of the box, contain-
measurements, as outlined in Fig. 4(a) and (b), by using a standard thermistor mount that has been accurately calibrated by NBS for efficiency and reflection coefficient. The maximum input power to the thermistor mount is 10 mW; however, accurate power measurements up to 10 W can be made by using a 30-dB attenuator whose scattering parameters are known. The scattering parameters of this attenuator are measured during the calibration process. Once measurement port 1 is calibrated to measure power, it can be used to calibrate the other measurement port. The power calibration is transferred to the higher power ranges using a “bootstrap” procedure as described in [3]. The estimated systematic error in measuring power is 3.2 percent for power measurements on the low range (20 W), 3.7 percent on the midrange (20 to 200 W), and 4.2 percent on the high range (200 to 1000 W). A significant portion of this error is due to a 1 percent error in the measurement of the efficiency of the standard thermistor mount by NBS, plus a 2-percent error in the measurement of $S_{12}$ of the 30-dB pad.

The analyzer is calibrated for accurate reflection coefficient measurements, as outlined in the steps shown in Fig. 4(c) through (g). In steps (c), (d), and (e), various combinations of shorts and 50-Ω loads are connected to measurement ports 1 and 2. A male type N short is connected to measurements port 1, while a female type N short is connected to port 2. The reflection coefficient of the loads need not be known. The shorts are used to electrically establish the measurements ports, and are assumed to have a reflection coefficient of $-1$.

A precision impedance standard is used to calibrate the analyzer for phase, reflection coefficient, and impedance measurements. This standard is a length of precision coaxial transmission line as shown in Fig. 4(f). Unlike a lossy standard, such as a 50-Ω termination, a coaxial line can be used at high power levels without significant changes in its parameters due to self heating.

The purpose of the four impedances $Z_1$ (open), $Z_2$ (3-dB attenuator + short), $Z_3$ (short), and $Z_4$ (50-Ω termination) is to provide four terminations with substantially different reflection coefficients. The reflection coefficients of these terminations also need not be known. The measurement data obtained by switching these terminations plus the connections to the various measurements ports are sufficient to characterize the power absorption analyzer and account for imperfections in components, such as the directional couplers and transfer switches.
V. SYSTEM PERFORMANCE

Two different high-power RF generators were used to test the analyzer. The first of these, which covered the 100–220-MHz frequency band, was an amplifier driven by a frequency synthesized signal generator. Its frequency was stable to within a few hertz, and its output power could be controlled by software commands from the ANA computer. The second generator, which covered the 220–850-MHz frequency band, was a manually tuned high-power oscillator followed by a high-power amplifier. Its frequency had to be manually set, as did its output power. Frequency drifts of ±50 KHz were typical of this system. High-power bandpass filters were used on the output of both generators to reduce second and higher order harmonics. The attenuation of second-order and higher harmonics was greater than 50 dB, relative to the fundamental.

One test of the analyzer was its ability to accurately measure the reflection coefficient $\Gamma$ of a short. For Figs. 5 and 6, the reflection coefficient of a short was repeatedly measured over a 10-min period, at a frequency of 700 MHz, and with an incident power to the short of 20 W. The magnitude $|\Gamma|$ of the reflection coefficient is shown in Fig. 5, while the angle is shown in Fig. 6. As can be seen, the measurements were of the order of

$$|\Gamma| = 0.99986 \pm 0.00008$$

and

$$\text{Angle of } \Gamma = 179.96 \pm 0.03 \text{ deg.}$$

The change in the angle of $\Gamma$ with time was largely due to the expansion of the system's cables with increasing temperature.

Another check on the analyzer was to connect measurement ports 1 and 2 together and let the system measure the power absorbed at this junction, which ideally should be zero. Fig. 7 shows the results of such a test where the power absorbed at the junction is plotted as a function of time. The test frequency was 700 MHz and the incident power was 20 W. Over the 15-h measurement period the system showed

$$P_{\text{sample}} = 0.004 \pm 0.008 \text{ W}.$$  

Thus, the average fractional error in measuring absorbed power is 0.02 percent (0.004 W out of 20 W). The long-term drift of the system was largely due to room temperature changes. Also, some of the cyclic behavior in the data was caused by the room's heating and cooling system, which was cyclic with a period of approximately 30 min or greater.

The power absorption analyzer was tested using a TEM cell 2 m long, 60 cm high, and 1 m wide. The manufacturer's specifications for the frequency response of this cell are dc to 250 MHz. However, care had to be excised, in that undesirable propagation modes could be excited at certain specific frequencies above 174 MHz [9]. A test frequency of 200 MHz, as used in this report, was above the first undesirable TE$_{101}$ resonance that occurs near 184 MHz, and was therefore suitable for tests with the
power-absorption analyzer. For the first measurement, the TEM cell was empty and the analyzer’s ability to determine that $P_{\text{sample}} = 0$ was tested. Fig. 8 shows a plot of $P_{\text{sample}}$ versus time for an 11-min period. The power incident to the cell ($P_i$) during this test was 1000 W and the frequency 200 MHz. The tests showed

$$P_{\text{sample}} = -0.25 \pm 0.4 \text{ W}$$

which results in an average fractional error of 0.025 percent (0.25 W out of 1000 W).

For the next set of tests, two plastic bottles of 1-percent saline solution, 300 g each, were inserted into the TEM cell. Each bottle was enclosed in a polyfoam insulated box with 1-in-thick sides. The incident power to the TEM cell was 500 W and the frequency 200 MHz. Fig. 9 shows a plot of the absorbed power versus time for a 90-min test period. The sample was in the cell only during the periods $t_1$ to $t_2$, and $t_3$ to $t_4$. At all other times, the cell was empty. Ideally, the absorbed power should be zero when the cell is empty. Fig. 9, however, show that the empty cell measurements drift away from zero with increasing time. The maximum drift of the empty cell measurements was 1 W and was highly correlated with the change in temperature of the room housing the experiment. At least part of this drift was believed to be due to a change in the power absorbed by the 7.32-m (24 ft) of 0.953-cm (3/8 in) flexible cable that connected the TEM cell with the measurement system. A plot of the room temperature during the experiment is shown in Fig. 10. If the empty cell drift is subtracted from the measurements, then the power absorption of the sample is found to be 3.4 W.

A graph of the magnitude $|\Gamma_i|$ of the reflection coefficient looking into the cell is shown in Fig. 11. The perturbations at 47 min into the test are caused by the operator. A plot of the incident power $P_i$ is shown in Fig. 12. The power absorption analyzer tried to maintain the incident power constant by adjusting the generator output power by software command. This “software power leveling” occurred approximately once per minute and was designed to remove the gross power changes caused by the amplifier drifting with temperature. With software leveling, the incident power remained constant to within 2-percent or better.

A check, as shown in Fig. 9, can be made on the measurements of absorbed power by using an independent calorimetric method [10]. The calorimetric method estimates the power absorbed by a 1-percent (by weight) saline solution to be

$$W = \frac{69.77 \times w (T_2 - T_1)}{(t_2 - t_1)}$$

where

- $W$ = net power absorbed by the solution, W
- $w$ = mass of solution, kg
- $(T_2 - T_1)$ = temperature increase of solution, °C
- $(t_2 - t_1)$ = elapsed time of experiment, min.
TABLE I

COMPARISON OF ABSORBED POWER MEASUREMENTS USING
THE POWER ABSORPTION ANALYZER AND CALORIMETRY

<table>
<thead>
<tr>
<th>Measurement Number</th>
<th>Absorbed Power as Measured</th>
<th>Absorbed Power as Measured</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>by the Analyzer (watts)</td>
<td>by calorimetry (watts)</td>
</tr>
<tr>
<td>1</td>
<td>3.4</td>
<td>3.4</td>
</tr>
<tr>
<td>2</td>
<td>3.4</td>
<td>4.6</td>
</tr>
<tr>
<td>3</td>
<td>3.6</td>
<td>3.9</td>
</tr>
<tr>
<td>4</td>
<td>3.7</td>
<td>3.8</td>
</tr>
<tr>
<td>Averages</td>
<td>3.6</td>
<td>3.7</td>
</tr>
<tr>
<td>Std. Deviations</td>
<td>0.13</td>
<td>0.32</td>
</tr>
</tbody>
</table>

Measurements, such as shown in Fig. 9, were repeated on four different occasions. The agreement between power absorption measurements as made by the analyzer and calorimetry is summarized in Table I.

The data shown in Fig. 9 are measurement number 2 in the table. It should be noted that the system drift, as evidenced by the nonzero $P_{sample}$ measurements when the TEM cell is empty, is subtracted from the data.

The averages of the four measurements using calorimetry and the power absorption analyzer agree to within 0.1 W (3.7–3.6 W). Since the incident power during the tests was 500 W, the average fractional error was 0.02 percent. Unfortunately, there were a number of factors that lead to questions regarding this agreement. One problem, that was not discovered until after the tests had been made, was that the rubber stoppers used to seal the plastic bottles absorbed RF power. Subsequent tests showed that the power absorbed by those stoppers was about 1.4 W (0.7 W each). Since the solution was in contact with the stoppers, it was not known how much heat energy, if any, was transferred to the solution from the stoppers.

Also, the spread in the calorimetry data, as evidenced by the 0.9-W standard deviation, showed the difficulty encountered in making repeatable calorimetry measurements.

In summary, the measurements show that an absorbed power on the order of 0.02 to 0.05 percent of the incident power can be measured with the power-absorption analyzer. To achieve this level of performance, the room housing the analyzer and TEM cell must be temperature stabilized to better than 1°C, or alternately the effects of temperature change must be taken into account by periodically removing the test sample from the cell, so that changes in the power absorbed by the empty cell and connecting cables can be monitored.

VI. Summary

A power absorption analyzer is described that makes accurate and repeatable measurements of the RF power absorbed by biological samples that are irradiated in a TEM cell. The analyzer operates over a power range of 1 to 1000 W and a frequency range of 100 to 1000 MHz. Experiments show that an absorbed power on the order of 0.02 to 0.05 percent of the incident power can be measured with the system. To achieve this level of performance, the temperature of the room housing the analyzer, cables, and TEM cell must be temperature controlled to better than 1°C. If the room is not temperature stabilized, then the biological sample must be periodically removed from the cell so changes in the power absorbed by the empty cell and connecting cables can be monitored. The estimated systematic error in measuring power is 3.2 percent on the low power range (20 W), 3.7 percent on the midrange (20 to 200 W), and 4.2 percent on the high range (200 to 1000 W). Test results show good repeatability in measuring the power absorbed by 300 g of 1-percent saline solution at 200 MHz and 500 W to the cell. The average power absorbed as measured by the analyzer is 3.6 W, with a standard deviation of 0.13 W. This measurement is also in good agreement with measurements using calorimetry techniques, which estimated the absorbed power to be 3.7 W.

ACKNOWLEDGMENTS

The authors are indebted to the contributions of A. Dudler and J. Yehle in assembling and testing the measurement system.

REFERENCES


John R. Juroshek was born in Sheridan, WY, on January 7, 1940. He received the B.S. and M.S. degrees in electronic engineering from the University of Wyoming, Laramie, in 1961 and 1962, respectively. In 1966, he attended the University of California, Berkeley, for a year of postgraduate study in communications theory. From 1962 to 1963, he was employed with the Federal Aviation Agency. In 1963, he joined the staff of the Department of Commerce at Boulder, CO. Since that time, he has worked with the
Probing Electromagnetic Fields in Lossy Spheres and Cylinders

GARY H. WONG, STANISLAW S. STUCHLY, SENIOR MEMBER, IEEE, ANDRZEJ KRASZEWSKI, AND MARIA A. STUCHLY, SENIOR MEMBER, IEEE

Abstract — Distributions of electric fields in lossy spheres and infinite lossy cylinders simulating biological objects were measured at 350, 920, and 2450 MHz. The measurements were performed in a computer-controlled scanning system using three different implantable nonperturbing probes. The results are compared with theory, and use of lossy spheres and cylinders for calibration of implantable probes is quantitatively evaluated.

I. INTRODUCTION

Dosimetry of electromagnetic fields is essential in quantifying biological effects of these fields and developing exposure standards for humans. Dosimetry is concerned with the determination of the electric-field intensity and the rate of energy deposition in biological bodies and their electrical models. The rate of energy deposition is defined as the specific absorption rate (SAR) usually expressed in W/kg [1]. The SAR is directly related to the intensity of the electric field in situ and the electric properties of the tissue.

Considerable progress in theoretical and experimental dosimetric methods has taken place in recent years, as reviewed elsewhere [1]–[3]. Lossy dielectric spheres serve as convenient models of biological bodies and their parts [1]–[3]. These models are relatively easy to analyze theoretically and to construct for experimentation. They also provide adequate simulation of some biological systems under certain exposure conditions [1].

The distribution of electric fields in a lossy sphere was previously obtained theoretically [4], and a computer program was developed [5]. Qualitative experimental verification was obtained [6]; however, a quantitative analysis of the accuracy with which the electric-field distribution can be measured by implantable electric-field probes is wanted. The SAR distribution was also measured by the thermographic technique [7].

The electric fields in lossy cylinders were determined analytically for an infinite cylinder [8] and analytically and experimentally for cylinders of finite length [9]. In the latter case, the experimental technique used had serious limitations when used for cylinders of small diameters.