The Planner Ensemble: Motion Planning by Executing Diverse Algorithms

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Abstract— Autonomous systems that navigate in unknown environments encounter a variety of planning problems. The success of any one particular planning strategy depends on the validity of assumptions it leverages about the structure of the problem, e.g., Is the cost map locally convex? Does the feasible state space have good connectivity? We address the problem of determining suitable motion planning strategies that can work on a diverse set of applications. We have developed a planning system that does this by running competing planners in parallel. 

In this paper, we present an approach that constructs a planner ensemble - a set of complementary planners that leverage a diverse set of assumptions. Our approach optimizes the submodular selection criteria with a greedy approach and lazy evaluation. We seed our selection with learnt priors on planner performance, thus allowing us to solve new applications without evaluating every planner on that application. We present results in simulation where the selected ensemble outperforms the best single planner and does almost as well as an off-line planner. We also present results from an autonomous helicopter that has flown missions several kilometers long at speeds of up to 56 m/s which involved avoiding unmapped mountains, no-fly zones and landing in cluttered areas with trees and buildings. This work opens the door on the more general problem of adaptive motion planning.

I. INTRODUCTION

The problem of designing a real-time motion planning system for an application is an open problem. It is currently solved by human intuition on what a good approach might be, picking one’s favourite planner and augmenting it with layers of heuristics for speedup. Surprising still, different groups come up with different solutions - e.g. compare the urban challenge approaches [1], [2]. Thus, there is a demand of a systematic approach to designing a planning solution that works best for the given application.

In this paper, our application was to design a motion planning system for an autonomous helicopter that has to fly smoothly in unknown environments that may span mountains, canyons and come into land avoiding buildings and trees. Fig. 1 shows two types of situations that can occur in the application. Given the requirement is for smooth paths, a trajectory optimization (such as CHOMP [3]) would be a natural choice. However, local minima (Fig. 1d) demand global reasoning - but one has to decide on the search space and search strategy of this global reasoning. One solution is to hand engineer a complicated solution that intelligently (using heuristics) decides what and when to optimize. Our approach was to run in parallel multiple complementary approaches and select the best one.

In this paper we present the planner ensemble. Each element in the ensemble is a planning algorithm with different parameters. The total size of this space is exponential in the number of algorithms, different modes of graph creation and different types of heuristics. We show that picking the best ensemble for an application is equivalent to optimizing a submodular criterion [4]. Since evaluating all possible planners on an application is expensive (even in offline cases), we resort to machine learning to learn priors on planning performance. These priors are used to determine the lazy evaluation of a planner.

Machine learning techniques have been used in [5] to learn the effectiveness of a global optimization, to predict trajectories in a new environment by learning from a database, and to predict the initial effectiveness of a trajectory for optimization [6]. The work closest to us is [7] in which machine learning is used to predict a sequence of options. Different learners are used for different slots - the marginal loss of selecting an action for one slot is handed as training data for the next slot. We differ by learning priors for each planner and computing the marginal gains explicitly - allowing us to add new planners and try new applications without having to retrain.

There is also a considerable amount of work on running planners in parallel to solve a motion planning task [8], [9].
Other works [11] use heuristics to adapt the search to the structure of the environment. A recent work [12] uses multiple inadmissible heuristics to guide a discrete graph search. We believe the approach introduced in this paper can be used to select effective heuristics given features about the environment.

We have already presented in [13] the details of our motion planning system for the autonomous helicopter. The reason behind the high performance of the system was because of the powerful combination of CHOMP [3] and RRT*-AR [14]. In this paper, we present a novel approach to automatically arrive at such a decision by characterizing performance of planners.

Our main contributions are:

- An ensemble of specialized planners that leverage diverse assumptions to maximize the performance of the system in an application.
- An automated ensemble selection that uses learnt priors on planner performance to create a custom set of planners for a given application.
- Results for the ensemble on an autonomous helicopter performing missions at high speeds.

II. PROBLEM STATEMENT

Let \( X \subseteq \mathbb{R}^n \) be the configuration space of the system. Let \( X_{obs} \subseteq X \) be invalid configurations that result in collision with obstacle. The dynamics of the system are specified as a dynamics constraint \( g(x, \frac{dx}{dt}, \ldots, \frac{d^r x}{dt^r}) \leq 0, x \in X \), where \( r \) is the relative degree. Let the trajectory \( \xi : [0, 1] \rightarrow X \) be a smooth mapping from time to configuration. The planning problem is to find the shortest dynamically feasible trajectory from start \( x_0 \) to the goal \( x_f \) that is collision free. This is expressed as follows:

\[
\begin{align*}
\text{minimize} \quad & \int_0^1 \|\dot{x}(t)\| \, dt \\
\text{subject to} \quad & x(0) = x_0 \\
& x(1) = x_f \\
& g(x, \frac{dx}{dt}, \ldots, \frac{d^r x}{dt^r}) \leq 0 \\
& x(t) \in X \setminus X_{obs}, t \in [0, 1]
\end{align*}
\]

We define an application as a distribution over different parameters of (1).

The success of a planner depends on the distribution of \( X_{obs} \). For example, there are configurations of \( X_{obs} \) which results in (1) being locally convex around an initial guess. In such situations, a trajectory optimization algorithm has a very high performance. There are also configurations of \( X_{obs} \) which result in a cluttered environment with low visibility, i.e., the straight line joining points far apart in the configuration space intersect \( X_{obs} \). In such situations, sampling based algorithms have degraded performance due to most of the connections failing during the collision check.

III. PLANNER ENSEMBLE

A. Overview

The central idea is to have an ensemble of planners running in parallel as shown in Fig 2. These planners work in parallel, often in a complimentary fashion, and bid their plans. These plans are then fed to a trajectory executive. The executive is a low latency verifiable unit whose job is to receive plans, ensure safety and send the best plan to the vehicle.

![Fig. 2: The Planner Ensemble](image)

B. Ensemble Generation

We first formalize the idea of an ensemble with the help of some supporting definitions. Let the database of all planners be \( \mathcal{P} \). A planner is an element \( P_i \in \mathcal{P} \). We use the definitions provided in [15] to define a planner. It can be thought of as a process operating on an implicit graph to make an explicit tree. For a discrete graph search, the implicit graph is a lattice with local connectivity. For sampling based algorithms, the implicit graph consists of points sampled from continuous space with a nearest neighbour ball to define connectivity. For trajectory optimization, the implicit graph is the continuous manifold. The explicit tree creation process varies between dynamic programming and some approximate versions. Heuristics are employed both in the implicit graph and explicit tree creation process. A survey of heuristics in sampling based motion planning literature is provided in [16]. We will delve into more details about \( P_i \) in subsection IV-A, but note that all such possible combinations imply \(| \mathcal{P} |\) is very large.

Let \( f \in \mathcal{F} \) denote a particular planning problem, i.e., an instance of (1). We define an application \( \mathcal{A} \) as a distribution over planning problems \( \Pr_{\mathcal{A}}(f) \).

Let \( s_i = \{0,1\} \) be the event of planner \( P_i \) finding a feasible solution, i.e., only satisfying the constraints in (1). Let \( \Pr(s_i | f) \) be the probability of this event for a planning problem \( f \). For deterministic planners, this reduces to an indicator function.

Let \( V_i(s_i, f) \in [0, 1] \) be the expected solution quality of \( P_i \) on \( f \) given the event \( s_i \). This is inversely proportional to the cost. In this work, we use \( V_i(1, f) = e^{-\beta \varepsilon_i} \), where \( \varepsilon_i \geq 0 \) is the expected suboptimality fraction of the solution and \( \beta \) is a scaling factor. Lack of a solution implies 0 score, i.e., \( V_i(0, f) = 0 \).

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Let $\Gamma \subset \mathcal{P}$ be an ensemble of planners. $\Gamma(i)$ refers to the $i^{th}$ planner in the ensemble. The optimization objective can be stated formally as

$$\begin{align*}
\text{maximize} & \quad \int_{\mathcal{P}} \hat{V}_t(f) \Pr_A(f) \, df \\
\text{subject to} & \quad |\Gamma| \leq B
\end{align*}$$

(2)

where $B$ is the budget of the ensemble and $\hat{V}_t(f)$ is the expected score of the ensemble of $f$. This can be expressed as

$$\hat{V}_t(f) = \sum_{s \in \Gamma} \max \{V_i(s_i, f)\} \Pr(s_i | f)$$

(3)

where $s_\Gamma = \{s_i : i \in \Gamma\}$ is a particular configuration of success/failures of the elements in the ensemble $\Gamma$, where the number of configurations is $2^{|\Gamma|}$.

There are two major reasons why the optimization is intractable. Firstly, the problem in (2) is NP-hard and the combinatorial approach has a worst case complexity $O(|\mathcal{P}|^B)$. Secondly, the evaluation of (3) is expensive since we don’t have analytical expressions for any of the terms. The evaluation involves sampling from $\Pr_A(f)$ and for each $f$, running the planners in the ensemble. In the next subsection, we present an approach to alleviate both of these problems.

C. Greedy Selection with Lazy Evaluation

As the problem is NP-hard, we present a greedy selection with lazy evaluation algorithm to optimize the criteria in (2). A greedy approach has a bounded sub-optimality guarantee as the criterion is sub-modular.

The objective is to select the best set $\Gamma^*$ on an application $\Pr_A(f)$ (2). Even though the setting is offline, since the space of planners $|\mathcal{P}|$ is large, not every element can be evaluated. If every element were to be evaluated we would get a table $s_i(f_i)$ and $V_i(s_i, f_i)$ for every planner $\mathcal{P}_i$ and sampled features $f_i$ from $\Pr_A(f)$. Greedy selection on this table would give a set with bounded sub-optimality.

Since the evaluation of (3) is expensive, we approach this problem by learning priors on the performance of each planner in $\mathcal{P}$. Let $f \approx f$ be an approximation of the planning problem $f$ in a feature space. The priors learnt are $\Pr(s_i | f)$ and $V_i(s_i, f)$. These priors allow us to analytically evaluate (3) without actually running the ensemble on the application. We will delve into the details of how these are learned in section IV.

Before we move on to the algorithm, we briefly comment on the assumptions made by the usage of priors. Firstly, $\Pr(s_i | f)$ and $V_i(s_i, f)$ incorporate the performance fluctuation due to approximation error of $f$, which we assume to be small given sufficiently expressive features. Secondly, we assume conditional independence of the success probabilities of the ensemble given the features, i.e., $\Pr(s_\Gamma | f) = \prod_{i \in \Gamma} \Pr(s_i | f)$. This assumption holds if the feature is expressive enough to represent the success of a planner without any other additional knowledge.

The algorithm we present greedily selects terms based on the marginal gains. Given an ensemble $\Gamma$, we define the analytical marginal gain of adding an element $e$ to this ensemble as

$$\Delta(e | \Gamma) = \int \left(\hat{V}_{\Gamma \cup \{e\}}(f) - \hat{V}_\Gamma(f)\right) \Pr_A(f) \, df$$

(4)

Algorithm 1 describes the lazy greedy approach. The application is initially sampled for a set of feature vectors $f_\mathcal{P}$. At each iteration, an approximation of (4) is estimated for every planner using the learnt priors and applying conditional independence. This step is orders of magnitude faster than running the planner on all the problems in $f_\mathcal{P}$. The planner with the largest marginal gain is selected and then the true marginal gain is computed by executing the planner on the application problems. The results of the trial are also used to update the priors for the planner. If the true marginal gain is still higher than the estimate of the next best planner, the planner is added to the ensemble.

IV. Learning Planning Performance Priors

A. Planning Strategies

In this work, we use the term planner $\mathcal{P}_i$ to imply a planning strategy. The core part of the planning strategy consists of applying a planning algorithm to solve the problem in (1). In addition, the strategy includes reductions and simplifications of (1) as well as leveraging assumptions about the structure of the problem.

Table I enlists the database of planners $\mathcal{P}$. Each planner was given 1.0s computation time. The first column indicates if the algorithms were optimizing the criteria or simply searching for a feasible option. The second column indicates the extent to which the planners attempted to satisfy the

<table>
<thead>
<tr>
<th>Planners</th>
<th>Optimizes</th>
<th>Constraints</th>
<th>Prediction Accuracy [%]</th>
<th>Regression Error (RMSE)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A*</td>
<td>Y</td>
<td>Dubins</td>
<td>80.61</td>
<td>0.071</td>
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<td>CHOMP</td>
<td>Y</td>
<td>Smoothness</td>
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<td>Dubins</td>
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<td>Dubins</td>
<td>84.01</td>
<td>0.099</td>
</tr>
<tr>
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<td>0.214</td>
</tr>
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</tr>
<tr>
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<td>Dubins</td>
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<td>Dubins</td>
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<td>SBL</td>
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<td>0.298</td>
</tr>
<tr>
<td>PSBL</td>
<td>N</td>
<td>None</td>
<td>78.91</td>
<td>0.301</td>
</tr>
</tbody>
</table>

1For readability, we will refer to $\mathcal{P}_i$ as $i$.
2This is similar to the set coverage function.
Algorithm 1 Planner Ensemble Selection

1: Input
2: \( \text{Pr}_A(f) \) : Application feature distribution
3: \( \text{Pr}(s_i | \hat{f}) \) : Learnt prior of feasibility
4: \( V_r(s_i, f) \) : Learnt prior of performance
5: \( B \) : Ensemble budget

6: Output
7: \( \Gamma \) : The selected ensemble

8: Variables
9: \( \Phi \) : Set of planners that have been evaluated
10: \( \rho(e) \) : Marginal gain of planner \( e \)

11: procedure LAZYGREEDY
12: \( \Gamma \leftarrow \emptyset \) \quad \triangleright \text{Initialize ensemble to empty set}
13: \( \Phi \leftarrow \emptyset \) \quad \triangleright \text{Initialize evaluated set to empty set}
14: \((\mathcal{F}_A, \mathcal{F}_E) \leftarrow \text{SAMPLE}(\text{Pr}_A(f)) \) \quad \triangleright \text{Sample from application to get set of planning problems and feature vectors}
15: \textbf{while} \: |\Gamma| < B \: \textbf{do}
16: \( \rho(e) \leftarrow \hat{\Delta}(e \mid \Gamma), \forall e \in \mathcal{P} \setminus \{\Gamma \cup \Phi\} \) \quad \triangleright \text{Compute marginal gain estimates using learnt prior applied on } \mathcal{F}_A
17: \( e \leftarrow \arg \max \rho(e') \) \quad \triangleright \text{Select planner with maximum marginal gain}
18: \( (\rho(e)) \leftarrow \text{EVALUATE}(e, \Gamma, \mathcal{F}_A) \) \quad \triangleright \text{Execute planner } e \text{ on application to get actual marginal gain}
19: \( \Phi \leftarrow \Phi \cup \{e\} \) \quad \triangleright \text{Add planner to evaluated set. This no longer needs to use priors.}
20: \textbf{if} \: \rho(e) < \rho(e') \: \forall e' \in \mathcal{P} \setminus \{\Gamma \cup e\} \: \textbf{then}
21: \( \Gamma \leftarrow \Gamma \cup \{e\} \) \quad \triangleright \text{Check if } e \text{ is still the best planner}
22: \textbf{end procedure}

Constraints - we note the fact that none of these planners were designed to fully satisfy the constraint \( g(\ldots) \) in (1) in their original form. Instead they either attempted to find a smooth solution, or a solution that satisfied Dubin’s dynamics or no constraints at all. We then use a fast non-linear projection operator approach, Dynamics Projection Filter [13], to project the solution on the constraint manifold.

To allow CHOMP to solve the problem, we created a distance field extending beyond \( X_{obs} \) to allow gradients to guide it out of collision. The smoothness term was used to allow solutions to satisfy \( g(\ldots) \) as much as possible before projection. RRT*-Tunnel is a variant of RRT* [17] that samples in the \( \mathbb{R}^3 \) workspace in a tunnel around the analytic solution. The tunnel is an assumption about how far from the initial guess the optimal solution may lie. RRT*-Obs is another variant of RRT* that samples on the obstacle manifold. The planners that did not attempt optimization were post-processed to get smooth outputs. We used the open source OMPL [18] for most of the planners other than CHOMP and A*.

B. Features

The feature vector \( \hat{f} \) consists of two components - global connectivity information and local distance field information.

1) Global Connectivity: A coarse lattice of fixed resolution spanning the whole workspace is created and centered on the line joining the start and goal. The feature vector is then \( \hat{f} = \{1(e \notin X_{obs})\} \) where \( 1(.) \) is the indicator function, \( e \) is the edge. This feature vector approximates the global connectivity of the workspace.

2) Local Distance Field: A dense lattice of fixed resolution of bounded volume around the straight line joining start and goal is created. For every vertex on this lattice, the distance field is sampled for the distance and direction to the nearest obstacle. This feature vector contains information about the local convexity of the objective and the obstacle density.

C. Training and Testing

Given the lack of standard training datasets in this area of work, we synthesized a dataset of 10000 planning problems by permutations and combinations of various scenarios that emphasize one or multiple major assumptions leveraged by an algorithm. Fig. 3 shows some samples from the dataset.

We used Random Forests [19] for learning success probabilities and performance of the planners because of their robustness to noise. To model the success probabilities, we used a discriminative classifier rather than learning a generative model for performance reasons. To get a model of planner performance, we did regression on the sub-optimality ratios. These ratios were obtained by running RRT* with a longer time budget and then taking the minimum cost incurred on a planning problem by any planner. The accuracy on the test dataset is shown in Table 1.

V. Ensemble Selection in Simulation

We used parameters of the model of Boeing Unmanned Little Bird (ULB) [13] with mission speeds of 30 m/s. We selected two contrary applications - Forest and City - and ran simulations with fully known and unknown (sensor limited) situation.
TABLE II: Ensemble selection for known forest application

<table>
<thead>
<tr>
<th>Planners</th>
<th>Iteration 1</th>
<th>Iteration 2</th>
<th>Iteration 3</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Prior (Eval)</td>
<td>Prior (Eval)</td>
<td>Prior (Eval)</td>
</tr>
<tr>
<td>A*</td>
<td>0.694</td>
<td>0.694</td>
<td>0.003</td>
</tr>
<tr>
<td>CHOMP</td>
<td>0.989 (0.681)</td>
<td>0.681</td>
<td>0.021 (0.069)</td>
</tr>
<tr>
<td>RRT*</td>
<td>0.700</td>
<td>0.700</td>
<td>0</td>
</tr>
<tr>
<td>RRT*-Tunnel</td>
<td>0.983 (0.848)</td>
<td>-</td>
<td></td>
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<td>RRT*-Obs</td>
<td>0.483</td>
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<td>0</td>
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<table>
<thead>
<tr>
<th>Ensemble</th>
<th>RRT*-Tunnel</th>
<th>RRT*-Tunnel</th>
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<tr>
<td>Slot 2</td>
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<td>CHOMP</td>
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</tr>
</tbody>
</table>

A. Known Environment

Fig. 3: Some samples of building blocks used to create the training dataset. Each scenario focuses on a particular strength/weakness that planners have. Permutations of these make a planning problem. (a) Pole - Locally convex (b) Wall - Non-convex, requires large excursion (c) Baffle - Local minima on either side, narrow entry passage. (d) Corridor - Start and goal halves of state space have only one small link (e) Bugtrap - Requires planners to search backwards (f) Various combinations of random environments

Fig. 4 shows snapshots from both applications. As the entire environment is known, the sensor plays no role. To clearly illustrate the ensemble selection process, Table II shows every step. Along with the priors, the actual value on evaluation is shown in brackets. In this case, RRT*-Tunnel and CHOMP were selected as the two planners. The lazy evaluation corrects for error in the estimation of the performance of CHOMP. The reason these two planners performed well is because the optimal solution was always within a tunnel of the initial guess and the cost function was usually convex around the initial guess. Fig. 4a is the output of CHOMP.

For the city application, we see in Table III that A* and RRT*-Tunnel were chosen. This is because this environment required reasoning in a global sense, discretization effects were acceptable and on occasion when the solution happened to lie near the initial guess, the RRT*-Tunnel was the only algorithm able to sample densely enough to get a solution as shown in Fig. 4b.

B. Unknown Environment

Fig. 5: Absence of a prior map makes the planning problem seem much easier. We illustrate the view of the robot as it explores the city. (a) The point cloud hits and misses correspond to seen obstacles and maximum range returns respectively. As far as the robot can see there is only a front wall, but once the front wall is revealed to the robot, it is for the most part easier, even convex around the initial guess on many occasions. This

In these environments, the environment was discovered on the fly by the sensor. Evaluation of a planner implies simulating with the sensor 3. According to Table III, the forest results remained unchanged but the city results were completely changed.

We examine this problem in Fig. 5. Since the city is incrementally revealed to the robot, it is for the most part easier, even convex around the initial guess on many occasions. This

3Making dataset dependent on prediction creates a data set distribution problem similar to [21]. We circumvent this for now by gathering datasets by running the offline planner.
TABLE III: Ensemble v/s individual performance for different applications

<table>
<thead>
<tr>
<th>Criteria</th>
<th>Ensemble Total</th>
<th>Ensemble Slot 1</th>
<th>Ensemble Slot 2</th>
</tr>
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<tbody>
<tr>
<td></td>
<td>Planner(Score)</td>
<td>Planner(Score)</td>
<td>Planner(Score)</td>
</tr>
<tr>
<td>Known Forest</td>
<td>RRT*Tunnel(0.85)</td>
<td>CHOMP(0.68)</td>
<td>0.92</td>
</tr>
<tr>
<td>Unknown Forest</td>
<td>RRT*Tunnel(0.72)</td>
<td>CHOMP(0.51)</td>
<td>0.85</td>
</tr>
<tr>
<td>Known City</td>
<td>A*(0.68)</td>
<td>RRT*Tunnel(0.59)</td>
<td>0.78</td>
</tr>
<tr>
<td>Unknown City</td>
<td>RRT*Tunnel(0.80)</td>
<td>CHOMP(0.54)</td>
<td>0.88</td>
</tr>
</tbody>
</table>

makes the use of A* wasteful when much higher quality solutions free of discretization effects can be obtained. The ensemble selection system is automatically able to leverage this assumption. We also see the effect of combining two planners in the forest environment leads to 18% improvement and within 85% of offline performance.

VI. AUTONOMOUS HELICOPTER FLIGHT

The planning system has been stress tested on an autonomous helicopter over a period of 4 months. Missions have ranged from avoiding no-fly zones, terrain obstacles and landing straight to ground while avoiding enroute trees, facing the wind direction and dealing with clutter at the landing zone. A detailed case-by-case analysis of these results can be found in [13].

For flight on an actual helicopter, we appended a collision avoidance objective, time to collision [13], which essentially penalizes high speed flight near obstacles and can scale naturally with speed. From the ensemble selection analysis, the planners selected were RRT*-Tunnel and CHOMP. We modified the RRT*-Tunnel to produce alternate routes (RRT*-AR [14]).

Fig. 6 shows an example of avoiding a mountain in one of the missions. This was a typical situation where CHOMP produces a high quality solution while the RRT*-Tunnel produces paths in the vicinity of the optimal solution. On another very similar mission in the same environment, a completely opposite situation was faced as shown in Fig. 7. Since the system was told to pass between a mountain and no fly zone, it got stuck in a poor local minima and the RRT*-Tunnel produced a path.

We also ran full system simulations on environments such as the grandcanyon (Fig. 8) and urban environment (Fig. 9). In the grandcanyon environment, CHOMP was selected 65.82% and RRT*-AR 34.18%. In the urban environment, CHOMP was selected 20.17% while RRT*-AR was selected 70.83%. The ensemble was able to keep the vehicle safe and successfully complete 100% of missions in these scenarios. The percentages indicate how the effectiveness of a planner changes throughout an application.

VII. DISCUSSION

We have presented an approach to solve diverse planning problems with an ensemble of complementary planners. We designed an ensemble selection system based on a greedy approach with lazy evaluation using learnt priors of planning performance. We presented results in simulation and for autonomous helicopters where the ensemble had

![Image](image1.png)

Fig. 6: Flying around an unmapped mountain in Mesa, AZ. (a) Safety pilot’s view of the mountain (b) The gradient due to time to collision objective takes the trajectory away from the obstacle (c) The RRT*-AR optimal path avoids the mountain by a much larger distance than required. The RRT*-AR tree contains branches on either side of the cost valley (d) The log normalized cost function valley with distance from the mountain peak. The optimizer descends into the valley within 8 iterations. The RRT*-AR computes alternate routes lying on either side of the valley.

![Image](image2.png)

Fig. 7: Flying between a no-fly zone (NFZ) and an unmapped mountain in Mesa, AZ (a) The skid camera view of the scenario (b) The gradient due to the time to collision pushes the trajectory into the forbidden NFZ (c) The RRT*-AR tree is very diverse and contorts to find a near optimal trajectory (f) Comparison of the RRT*-AR trajectory to optimizer shows that RRT*-AR is safer

![Image](image3.png)

Fig. 8: Both RRT*-AR and Optimizer dominate interchangeably in a mission in the Grand Canyon (a) Optimizer dominates here because the gradients from the edges push it into a global minima (b) Optimizer gets trapped in a bad local minima in a space between two obstacles. RRT*-AR plans around the obstacle.
better performance on the mission than a single planner. Even though our approach shows promising results, there are several issues that make this a hard problem to solve.

The first issue concerns the noise in the learnt priors. The priors are learnt over a training distribution which is different from the application distribution. This makes it difficult to bound the performance of the selected ensemble from the best ensemble $\Gamma^*$. The approach used in [7], where a cascade of regressors are used may reduce the noise level. However the difference in distribution is still a key issue.

The second issue is that this approach does not address an online setting. In the online setting, the algorithm is required to produce a different ensemble $\Gamma$ at every time step to bound the regret with respect to the best ensemble $\Gamma^*$ in hindsight. Since each element cannot be evaluated (as in weighted experts [22]), this must be framed as a multi-armed bandit problem [23]. In addition, the utilization of the features $f$ would allow for one to have a lower regret in comparison to not using the priors.

The third issue is with regards to a more complex matter of distributions. Not only is $\Pr_A(\gamma)$ unknown, it should also be a function of the selected ensemble $\Gamma$. This is because the planners dictate where the robot navigates and the kind of problems it is likely to encounter. Work done in [21] provides some potential direction for further research.

Another key source of difficulty is that the features must be able to capture all aspects of the environment in order to effectively predict planner performance. For practical purposes, this might be a very difficult function to learn. A more predictable property is to learn the interdependence among planners. When one planner is evaluated, this model can reliably predict the likelihood of success of a dependent planner. Work done on multi-armed bandits with dependence [24] shed some light on this matter.

VIII. ACKNOWLEDGEMENT

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