Optimizing the Ultrawide-Band Photonic Link

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Abstract—Performance of wide-band photonic links (PL’s) using Mach–Zehnder modulators (MZM’s) is reported. Comparison parameters include loss, noise figure, and spur-free dynamic range (SFDR). The feasibility of a 0-dB noise-figure link even with passive matching is given and the advantages of dual-output MZM’s are presented. A new figure of merit is introduced to quantitatively optimize link performance with or without a preamplifier.

Index Terms—Cascade systems, impedance matching, intensity modulation, intermodulation distortion, optical fiber delay lines, sensitivity.

I. INTRODUCTION

As the use of photonic links (PL’s) increases in wide-band microwave systems, the capabilities of such links in terms of sensitivity and dynamic range become critical. Existing assessments of link performance [1]–[3] do not sufficiently address the effects of broader bandwidths, higher photocurrents, lower relative intensity noise (RIN), modulator half-wave voltage, and external preamplifiers. In this paper, we expand the basic model presented heretofore to account for multioctave and balanced-detection PL’s. This model, combined with clear performance goals, highlights key design parameters in the PL as well as in the accompanying microwave components. By introducing a simple figure of merit which integrates sensitivity and dynamic range and applying it to cascaded systems, we quantify the tradeoffs which arise when the PL is interfaced with a microwave system. We also clarify the notion [1], [3], [4] that microwave PL’s are fundamentally limited to noise figures \( \geq 3 \) dB by input matching considerations.

In order to establish a baseline, we focus on unconditioned PL’s as opposed to links involving linearization schemes [5], [6]. Since state-of-the-art dynamic ranges are currently achieved using externally-modulated links, we consider these rather than direct modulation techniques. To simplify further, we look only at intensity-modulated direct-detection (IMDD) links where the output photocurrent is the baseband signal. Indirect alternatives are summarized in [7].

II. LINK NOISE

Noise power in IMDD links is typically dominated by three effects: thermal, shot, and intensity noise. Output thermal noise power comprises that created at the output of the link \( N_{th} = k_B T B \) and that created at the input to the active portion and amplified by subsequent link gain \( N_{t} = k_B T B G / G_m \), where \( k_B \) is Boltzmann’s constant, \( T \) is temperature, \( B \) is the receiver bandwidth, \( G \) is the RF gain of the entire PL, and \( G_m \) accounts for passive impedance matching to the modulator RF input. Shot and intensity noise depend on detected optical power, detection scheme, and photodetector (PD) impedance matching. The outputs of dual-output (\( X \)-coupled) Mach–Zehnder modulators (MZM’s) carry the same IM signal 180° out of phase allowing a balanced-detection scheme [8]. The photocurrents for the single-output (\( Y \)-coupled) MZM and for each arm of the \( X \)-coupled MZM are

\[
\begin{align*}
i_Y &= i \left[ 1 + \cos(\Delta \phi_Y + \phi_m(t)) \right] \\
i_{X \pm} &= \frac{1}{2} i \left[ 1 \pm \cos(\Delta \phi_X + \phi_m(t)) \right]
\end{align*}
\]

where \( i \) is the total dc photocurrent at quadrature, \( \Delta \phi_Y \) is the static phase shift between arms, \( \phi_m(t) \) is the modulated phase, and \( \Delta \phi_X \equiv \Delta \phi_Y - \pi / 2 \) yields a similar functional form in the balanced coupler case. Although PD nonlinearities are typically present above ~1 mA of photocurrent [9], for this paper we exclude these effects.

The output shot noise power [10] is proportional to the total photocurrent

\[
N_{sY} \approx 2e |t| R_B (1 + \cos \Delta \phi) \quad N_{sX} = 2k_B e |t| R_B
\]

where \( e \) is electronic charge, \( R_B \) is the system load (or source) impedance, and \( k_B \) is an output impedance-match correction. The correlated-intensity noise power from each PD of the balanced detector coherently subtracts, assuming path lengths from modulator to detector and PD amplitude responses are well matched. Therefore, the intensity noise power [11] is given by

\[
\begin{align*}
i_{Y} &\approx k_B e t_B (1 + \cos \Delta \phi) \\
i_{X \pm} &\approx \frac{1}{2} k_B e t_B (1 + \cos 2\Delta \phi)
\end{align*}
\]

where \( t_B \) is the RIN. The approximation symbols used in the above expressions indicate that the small-signal approximation is being used.

III. GAIN, NOISE FIGURE, AND LINEARITY

To quantify these parameters, we assume \( \phi_m = \phi (\cos \omega t + \cos \omega_2 t) \) where \( \phi = \pi \sqrt{2k_B T B} / \nu_0 \), \( P \) is the input RF power to the MZM, and \( \nu_0 \) is the half-wave voltage. Noting that the photocurrent in the balanced detector configuration is the difference of \( i_{X \pm} \) in (1), we evaluate the photocurrent using...
Bessel functions [12] shown in (4) at the bottom of this page, where only sum terms are used for harmonics. Noting that the performance of the X-coupled PL should be compared to that of the Y-coupled PL at half the current (same optical source power), the small-signal RF gain can be written using the same expression for both coupling configurations as follows:

$$G = k_B k_{\text{eff}} (\pi i R_q \sin \Delta \phi / v_T)^2.$$  (5)

For low $v_T$ (high gain), thermal noise at the MZM RF input contributes significantly to output noise which, for a passively-matched input, is thereby independent of $k_B k_{\text{eff}}$. For active matching, thermal noise at the input to the matching network must also be considered.

Since noise figure is defined [13] as

$$F \equiv \frac{\text{total output noise}}{G k_B T B} = \frac{N}{G k_B T B}$$  (6)

the PL noise figure approaches 0 dB if the modulator input is impedance matched with negligible loss and $N_{IT} \gg N_{TR} + N_s + N_I$. But practically, as shown in Fig. 1, RIN limits the sensitivity which can be obtained [14]. (In all figures, the following are assumed unless otherwise indicated: $k_{\text{in}} = 1$, $f_s = 0.1$ fs (−160 dB/Hz), $R_T = 50 \Omega$, $T = 300 \text{ K}$.) Note that the noise figure of a quadrature-biased Y-coupled PL with a −170 dB/Hz RIN source and 10-mA photocurrent can actually be improved by 4 dB using balanced detection. Also, the X-coupled link data in Fig. 1 and the remainder of this paper assumes ideal RIN cancellation as in (3). In a practical sense, balanced detection offers at least 20 dB of suppression: at high $f_s$, the performance indicated by a particular Y-coupled curve in Fig. 1 can be achieved by an X-coupled PL using an optical source with roughly 20 dB greater RIN.

It has been asserted [4] that, for a “lossless passive matching” network, the modulator input matching resistor contributes an additional $k_B T B$ such that the fundamental noise figure limit is 3 dB. In contrast, we consider such a resistor to be integral to the matching network which, therefore, is lossy, gives $k_{\text{in}} < 1$, and from $N_{IT} = k_B T B C/k_{\text{in}}$ results in a $> 0$ dB noise-figure limit. Note that for a traveling-wave modulator at traveling-wave frequencies, the noise generated by a matching resistor (at the RF output of the modulator electrodes) is counterpropagating to the optical wave. Hence, its modulation efficiency is severely reduced, leading to $< 3$-dB noise figure. Also in principle, a modulator can be designed to deliver RF input power to an antenna so that no terminating resistor is needed, and again, the noise figure would be $< 3$ dB. In addition, we point out that impedance mismatch may be traded off for ultralow noise figure in some cases.

In a multioctave bandwidth, either second- or third-order intercet powers (IP’s) can become the limiting distortion terms depending upon MZM bias. Using small-signal approximations in (4), the output second- and third-order intermodulation IP’s (OIP2 and OIP3) are [15]

$$P^{(2)} \approx 2 k_{\text{eff}} R_q \sin^2 \Delta \phi \sin^2 \Delta \phi,$$

$$P^{(3)} \approx 4 k_{\text{eff}} R_q \sin^2 \Delta \phi \cos \Delta \phi.$$  (7)

This and other previous expressions are fairly well known and serve as background for the remainder of this paper.

IV. SPUR-FREE DYNAMIC RANGE AND PERFORMANCE COMPARISONS OF ALTERNATIVE PL CONFIGURATIONS

Combining small-signal output noise power and intercept values, we have

$$R_Y \approx \min \left[ \frac{P^{(2)}}{N_Y}, \frac{P^{(2)}}{N_X} \right]$$

$$R_X \approx \min \left[ \frac{P^{(3)}}{N_X}, \frac{P^{(3)}}{N_X} \right]$$

$$N_Y = N_{TR} + N_{IT} + N_{sY} + N_{sX},$$

$$N_X = N_{TR} + N_{IT} + N_{sX} + N_{sX}$$  (8)

where $R$ is the spur-free dynamic range (SFDR). While the single-octave $R_Y$ is well known [5], the multioctave expressions extend the model to include second-order distortion contributions from all even-order terms of the link transfer function Taylor expansion. Indeed, a more complete nonlinear model is expressed by $R \approx \min [(P^{(n)})/(N^{(n−1)})/(n)]$ [6] where $n$ is the distortion product order. The expressions for $R_X$ further extend the model to balanced PL’s. Fig. 2 illustrates (8) versus bias for PL’s with the same optical source power. An additional curve shows the relative insensitivity of the

\[
\begin{align*}
i_Y &= i + i_X \\
i_X &= i \times \begin{cases} 
\frac{J_0(\phi) \cos \Delta \phi}{2(1-\frac{m+n}{2})} & m = n = 0 \\
\frac{J_m(\phi) J_n(\phi) \cos \Delta \phi \cos(m \omega_1 \pm n \omega_2) t}{2(1-\frac{m+n}{2})} & m + n \text{ even} \\
\frac{J_m(\phi) J_n(\phi) \sin \Delta \phi \cos(m \omega_1 \pm n \omega_2) t}{2(1-\frac{m+n}{2})} & m + n \text{ odd}
\end{cases}
\end{align*}
\]
standard low-current single-octave PL to MZM bias. As bias is varied, more or less optical power is transmitted changing both \( N \) and \( P^{(n)} \). Note that, in a multi octave system, the SFDR is described by the IP2-related value except near quadrature, where the limiting value is IP3-related.

There are a number of conclusions to be drawn regarding unconditioned PL’s from (8). First, in a balanced-detection system, the optimum bias is quadrature. As \( B \) increases and the SFDR is reduced, the relative separation between the IP3- and IP2-related curves decreases somewhat so that the range of acceptable bias points near quadrature widens. Second, the multi octave single-output link SFDR (also optimized at quadrature) has an upper limit with increasing photocurrent approximated by a simple expression: \( R_{3y}|_{\pi/2} \approx (4/B_{y})^{2}/3 \). Third, in a single-octave single-output IMDD link, optimum bias approaches 180° with increasing photocurrent; this is the “low-biasing” method [2]. The optimum bias is found analytically to satisfy the following relation:

\[
1 + \cos \Delta \theta = \frac{\sqrt{b^2 + 4be + 4b^2} - b}{2e + 2b} \tag{9}
\]

where \( b \equiv k_{b}I_{c}/k_{B}nR_{T} \). This relation and the photocurrent at optimum low bias are pictured for various RIN in Fig. 3. Note that, for increasing \( t_{c} \), the photocurrent must be clamped at lower values to retain thermal- or shot-limited noise, comparable to that of the balanced PL.

Since the OIP3 expression is the same for both \( X \)- and \( Y \)-coupled configurations, the low-biased single-octave PL SFDR will be comparable to that of the balanced PL as shown in Fig. 4 along with the RIN-limited quadrature-biased \( Y \)-coupled PL. However, there are practical disadvantages with low-biasing. First, unlike a balanced PL, the low-biased PL does not offer shot-noise limited SFDR in a multi octave system. Second, low-biased links suffer increased link loss relative to balanced-detection PL’s according to (5). As shown in Fig. 5, the gain increase due to higher optical source power is partially undercut by MZM transmission loss in the low-biased link. Again, the SFDR or gain of the balanced-detection PL should be compared to that of the \( Y \)-coupled PL at half the current; increasing photocurrent from 1 to 100 mA in the balanced-detection scheme reduces the loss by 40 dB, whereas increasing it from 0.5 to 50 mA in the low-biased scheme results in only a 26.3-dB improvement. Thus, at high \( i \), the \( Y \)-configured link requires more preamplifier gain to achieve given net link gain and, thereby, risks SFDR reduction. Also, low-biased link RF gain decreases with increasing \( t_{c} \) due to (9), degrading its sensitivity.
A third disadvantage of the low-biased PL is that SFDR, link gain, and transmitted photocurrent are very sensitive functions of MZM bias. As shown in Fig. 2, at 50 mA, the bias approaches the transmission null of the MZM. On the side of the peak facing away from the null, a 10$^\circ$ error reduces SFDR by 0.9 dB. But on the null side, the same error reduces SFDR by 10.1 dB. The same errors in the 100-mA balanced link reduce SFDR by only 2 dB. A ± 5° error in the 100-mA balanced link causes the gain to vary by 8.6 dB and the photocurrent to vary by a factor of 7.4, making the link orders of magnitude more sensitive to bias drift or thermal noise at the bias input to the MZM and, in the worst case, risking PD failure due to high current. Finally, recalling that $\Phi$ differs from its small-signal value when the MZM is off quadrature, it is apparent that the low-biased link will generally have more noise, less dynamic range, and less RF link gain than indicated by Figs. 4–6. This is particularly true for high $\Phi$ PL’s because the bias is so close to the null that the small-signal approximation conditions [used for (2), (3), (5), (7), and (8)] are never met. For these reasons, we conclude that the balanced configuration PL makes better use of optical source power and, therefore, we will limit subsequent discussion to these links.

V. OPTIMIZING THE PHOTONIC LINK

It has been shown [1] that reduced $v_{\pi}$ can eventually reduce PL SFDR. Sensitivity requirements sometimes necessitate this penalty in favor of lower noise figure. Similarly when choosing preamplifiers with the same noise figure and OIP3, but differing RF gain, (6) and (8) imply that the higher gain amplifiers will necessarily have lower SFDR. Improved PL sensitivity requires less preamplifier gain to achieve overall sensitivity and can, therefore, improve overall dynamic range. To quantify these tradeoffs, we consider three scenarios: minimum specified SFDR, maximum specified noise figure, and simultaneously optimized SFDR and noise figure. For simplicity, we also consider only single-octave systems.

For two-port devices, the dynamic range of a cascade is never greater than that of the lowest dynamic range component provided the output noise of all components except the last is much greater than thermal noise. This is easily seen if (8) is computed using the noise-figure equation [13] and the expression for cascading distortion OIP’s [15]

$$\frac{1}{P_{\text{in}}^{(3)}} = \frac{1}{G_2(I_1^{(3)}) + \frac{1}{I_2^{(3)}}}$$

(10)

Since the PL is essential, one tries to meet the specifications first by optimizing the PL and then by including a preamplifier if necessary. Note that conditioned links involve a linearization scheme which invalidates the second expression in (10) because of nonzero phase between distortion products in each component, eliminating the constraint on net SFDR. Distortion cancellation can be taken into account [5], [15] and the conditioned PL treated as a single component with set values of $G$, $F$, and $P$, in which case the following analysis regarding preamplifier selection is still valid.

A. Minimum SFDR Specified

We assume a technological limitation $i_{\text{max}}$ because, as we have seen, $R$, $F$, and $G$ improve with increased $i$. The maximum SFDR requirement which can be met by the PL (and, therefore, the cascaded system) is given by (8) with $i = i_{\text{max}}$ and $v_{\pi} \to \infty$. It may seem odd that maximum SFDR is obtained for a modulator with maximum conversion loss, but this is simply because such a device can handle more input power without distortion. If the SFDR requirement is less than this maximum value, then the optimum value of $v_{\pi}$ is the least value which will meet the requirement because this value will produce the lowest noise figure. Preamplifiers need not be discussed due to the “bottleneck” described above: if the SFDR requirement is not met, there is no way to meet it using another device; if it is met, adding a preamplifier reduces the SFDR. One might argue that reducing $R$ could be traded for lowering $F$; however, this means SFDR is not really a hard requirement and the third scenario below is better suited to solving the problem.

B. Maximum Noise Figure Specified

In the second scenario, we divide possible values of $v_{\pi}$ into two regions: the low values satisfying a minimum $F$ requirement and the high values which necessitate a preamplifier to meet it. If minimum preamp gain $G_{\text{min}}$ is used in the latter case, the output noise is independent of $G_{\text{min}}$ and depends on PL gain only to the extent that $k_{\text{in}}$ departs from unity

$$N_{12} = \frac{F_{12}}{F_{12} - F_1} \left\{N_s + k_BTB \left[1 + \frac{G_2}{k_{\text{in}}(1 - k_{\text{in}})}\right]\right\}.$$  

(11)

As a result, for nearly-lossless input impedance matching, $R$ has the same logarithmic dependence on $v_{\pi}$ as the cascaded
OIP3. This is demonstrated in Fig. 6 where < 3-dB noise figure is specified. The discontinuity represents the boundary between the two \( \nu_\pi \) regions. To satisfy the requirement with increasing \( \nu_\pi \), larger preamplifier gain is required reducing preamplifier SFDR and, thereby, system SFDR. The SFDR will be optimized for the largest value of \( \nu_\pi \) where the noise-figure requirement is met by the PL alone.

C. Optimizing Both Noise Figure and SFDR

In the third scenario, we resolve the tradeoff between dynamic range and sensitivity directly by defining a figure of merit: \( M \equiv R/F \). The dependence of this quantity on all link parameters except \( \nu_\pi \), as shown at (8) follows that of SFDR. For example, since \( R \) increases and \( F \) decreases with increasing \( i_\pi \), \( M \) will also increase. One can also show that the optimum bias values are as previously stated using the following arguments.

In the dual-octave case, the tangent dependence in (7) of the OIP2 dominates so that the optimum bias is quadrature. In the single octave case, \( 1/F \) and \( F^{3/2} \) have the same functional dependence on \( \Delta \phi \) because \( F^{3/2} \) and \( G \) have the same functional dependence on \( \sin^2 \Delta \phi \). As a result, the balanced configuration is optimized at quadrature as before and the optimum bias in the \( Y \)-coupled configuration is again described by (9).

The utility of the figure of merit becomes apparent when we compute the optimum value of \( \nu_\pi \). Since \( \nu_\pi \) only enters (8) through the quantity \( G \), we can answer this question by setting the derivative of \( M \) with respect to \( G \) equal to zero as follows:

\[
G_1^{(3)}_{G_2,0} = \frac{3}{2} [1 + (N_x + N_i)/kT] (12)
\]

In other words, increasing gain (decreasing \( \nu_\pi \)) above the value where \( N_x + N_i \) reduces \( M \) by decreasing \( R \) while decreasing \( G \) below this value reduces \( M \) by decreasing sensitivity. The additional factor of \( 3/2 \) is a consequence of the distortion order considered. For second-order dominated SFDR, this factor is 2; for SFDR dominated by \( n \)-th order distortion products, the factor is \( n/(n-1) \). Having determined the optimum \( \nu_\pi \), we can also use the merit to help us select a preamplifier. That is, the optimum preamp gain \( G_{1,0} \)...
VI. Conclusion

Photonic-link performance has been revisited and expanded. The passive input matching constraint on lowest achievable PL noise figure has been clarified. Quantitative results have been derived comparing single- and multi octave bandwidth low-biased and balanced configuration link performance and an exact relation for the low-biasing scheme has been presented. These comparisons reveal that low-biased PL performance is generally inferior to that of the balanced PL. Also, new insight into the problem of optimizing this performance over key design parameters of the PL itself and of an accompanying microwave preamplifier has been provided using a new figure of merit which simultaneously accounts for changes in noise figure and SFDR, allowing for quantitative analysis of the resulting tradeoffs.

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References


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